

Strong CP violation in spin-1/2 singly charmed baryons

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ABSTRACT: We report on the calculation of the CP-violating form factor F_3 and the corresponding electric dipole moment for charmed baryons in the spin-1/2 sector generated by the QCD θ -term. We work in the framework of covariant baryon chiral perturbation theory within the extended-on-mass-shell renormalization scheme up to next-to-leading order in the chiral expansion.

KEYWORDS: CP violation, Chiral Lagrangians, Effective Field Theories

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Contents

1	Introduction	1
2	Chiral Lagrangian including CP-violating terms	2
3	CP-violating electromagnetic form factor	5
4	Results	9
5	Conclusion	9
A	Scalar loop integrals	10
B	Loop contributions	10
C	Results for the CP-violating form factor	14

1 Introduction

Charge conjugation and parity symmetry (CP) violation is an essential condition for an asymmetry between matter and anti-matter in the present universe. On the other hand, CP violation by the complex phase of the Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix is insufficient to explain the dominance of matter over antimatter [1, 2], meaning that the presence of other CP violating mechanisms within or beyond the Standard Model (SM) is required. The QCD θ -term is the only source of P and T violation within the SM beyond the complex phase of the CKM quark-mixing matrix. However, because of the significant suppression of electric dipole moments (EDMs) induced by the complex phase of the CKM matrix and unobservably small CKM backgrounds, any measurement of EDM of any quantum system would indicate of presence CP violation beyond the CKM mechanism in the SM. EDMs are important observables generated by the CP-violating effects. Thus, measurements of hadron EDMs lead to severe restrictions in the mechanism generating CP violation, as detailed e.g. in ref. [3].

CP violation has recently been established in the charm sector, more precisely in the meson decays $D^0 \rightarrow K^- K^+$ and $D^0 \rightarrow \pi^- \pi^+$ [4], and LHCb has also measured the difference of CP-asymmetry of the three-body singly Cabibbo-suppressed Λ_c^+ decays [5]. There have also been quite a number of studies predicting CP asymmetries in charmed baryon decays, see e.g. [6] and references therein. It is therefore of interest to investigate other possible effects of CP violation in singly-charmed baryons. Indeed, a first measurement of CP violation in $\Xi_c^+ \rightarrow p K^- \pi^+$ decays has been performed by LHCb [7]. However, these data are consistent with the hypothesis of no CP violation. On the other hand, another experimental study promises to search for direct CP violation by measuring the asymmetries of three different decay channels of the Λ_c^+ baryon [8].

Here, we concentrate on the effects generated by the strong CP-violating θ -term of QCD, that also induces electric dipole moments in light baryons, as pioneered in

refs. [10, 11]. The proper framework to address such questions is baryon chiral perturbation theory, see [12] for a review. In fact, the masses, axial charges, and electromagnetic decays of the charmed and bottomed baryons have already been calculated in the framework of the heavy baryon approach [13, 14]. More recently, the magnetic moments of the spin-1/2 singly charmed baryons were analyzed in covariant baryon chiral perturbation theory [15]. In this paper, we extend these studies and work out the CP-violating effects induced by the QCD θ -term. While there is experimental activity to assess the effects of the θ -term in neutron and proton EDMs, singly-charmed baryons offer a completely new venue towards these elusive effects, with very different systematic uncertainties that hamper such measurements. How competitive these measurements will be would require a much more refined analysis as presented here. We note that recent progress towards the first measurement of the charm baryon dipole moments has been reported in ref. [9], thus our investigation is very timely. In the near future, further measurements with charmed hadrons, along with different theoretical improvements, would help to further elucidate the CP violation in the charm quark sector.

The manuscript is organized as follows. In section 2, we briefly discuss the underlying chiral Lagrangian. The CP-violating electromagnetic form factor of the singly-charmed baryons is worked out in section 3 followed by the display of our numerical results in section 4. Section 5 contains the summary and outlook. The appendices contain some technicalities as well as more detailed tables of results.

2 Chiral Lagrangian including CP-violating terms

The QCD Lagrangian of the strong interactions including the θ term reads

$$\mathcal{L}_{\text{QCD}} = \bar{q}(i\not{D} - \mathcal{M})q - \frac{1}{4}\mathcal{G}_{a\mu\nu}\mathcal{G}_a^{\mu\nu} + \frac{g^2\theta}{64\pi^2}\varepsilon_{\mu\nu\rho\sigma}\mathcal{G}_a^{\mu\nu}\mathcal{G}_a^{\rho\sigma}, \quad a = 1, \dots, 8, \quad (2.1)$$

where $\mathcal{G}_a^{\mu\nu}$ is the gluon field-strength tensor, g is the strong coupling constant and \mathcal{M} is the quark mass matrix. Strong CP violation arising from the U(1) anomaly in QCD is specified via the vacuum angle θ . The measurable quantity is not θ but the combination

$$\theta_0 = \theta + \arg \det \mathcal{M}, \quad (2.2)$$

because of the anomaly. Here, to describe the phenomena related to the θ -term, we seek a description in a properly tailored effective field theory, see e.g. refs. [16, 17] for the detailed construction of the corresponding effective Lagrangian to one loop accuracy.

The Goldstone bosons together with the flavor singlet η_0 , resulting from the spontaneous symmetry breaking of $U(3)_R \times U(3)_L$ into $U(1)_V$, are represented by the matrix-valued field \tilde{U} . Treating the vacuum angle $\theta(x)$ as an external field, it transforms as $\theta(x) \rightarrow \theta'(x) = \theta(x) - 2N_f\alpha$ under axial U(1) rotations, with N_f the number of flavors, and α is the rotation angle. Following the spontaneous chiral symmetry breaking, under the axial U(1) transformation, \tilde{U} changes but the combination of $\bar{\theta}_0(x) = \theta(x) - i \ln \det \tilde{U}(x)$ stays invariant. Using this invariant combination of $\bar{\theta}_0(x)$, one can construct the most general mesonic chiral effective Lagrangian up-to-and-including second chiral order

$$\begin{aligned} \mathcal{L} = & -V_0 + V_1\langle\nabla_\mu\tilde{U}^\dagger\nabla^\mu\tilde{U}\rangle + V_2\langle\tilde{\chi}\tilde{U} + \tilde{\chi}\tilde{U}^\dagger\rangle + iV_3\langle\tilde{\chi}\tilde{U} - \tilde{\chi}\tilde{U}^\dagger\rangle \\ & + V_4\langle\tilde{U}\nabla_\mu\tilde{U}^\dagger\rangle\langle\tilde{U}^\dagger\nabla^\mu\tilde{U}\rangle. \end{aligned} \quad (2.3)$$

Note that $\langle \dots \rangle$ denotes the trace in flavor space and $\tilde{\chi} = 2B_0\mathcal{M}$, with the light quark mass matrix $\mathcal{M} = \text{diag}(m_u, m_d, m_s)$. The covariant derivative of \tilde{U} is given by

$$\nabla_\mu \tilde{U} = \partial_\mu \tilde{U} - i(v_\mu + a_\mu)\tilde{U} + i\tilde{U}(v_\mu - a_\mu), \quad (2.4)$$

where v_μ and a_μ are the conventional vector and axial-vector external sources. The V_i coefficients in the Lagrangian (2.3) are functions of $\bar{\theta}_0$. One needs to determine the vacuum expectation value of \tilde{U} in order to include non-trivial vacuum effects based on the angle θ_0 . Parameterizing the vacuum as

$$U_0 = \text{diag}(e^{-i\varphi_u}, e^{-i\varphi_d}, e^{-i\varphi_s}), \quad (2.5)$$

the minimized potential energy $V(U_0)$ can be determined using the notation $\bar{\theta}_0 = \theta_0 - \sum_q \varphi_q$. In this way, the Taylor expansions of the V_i functions in terms of $\bar{\theta}_0$ yield

$$\begin{aligned} V_i(\bar{\theta}_0) &= \sum_{n=0}^{\infty} V_i^{(2n)} \bar{\theta}_0^{2n} \quad \text{for } i = 0, 1, 2, 4 \\ V_3(\bar{\theta}_0) &= \sum_{n=0}^{\infty} V_i^{(2n+1)} \bar{\theta}_0^{2n+1}. \end{aligned} \quad (2.6)$$

Note that while all other V_i are even function of $\bar{\theta}_0$, V_3 is odd. To express the Lagrangian in terms of the angles φ_q one then writes the \tilde{U} with the vacuum expectation value U_0 as $\tilde{U} = \sqrt{U_0}U\sqrt{U_0}$ by choosing

$$U = \exp\left(i\sqrt{\frac{2}{3}}\frac{\eta_0}{F_0} + i\frac{\sqrt{2}}{F_\pi}\phi\right), \quad (2.7)$$

where ϕ represents the Goldstone boson octet

$$\phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta_8 \end{pmatrix}.$$

Thus, the chiral effective Lagrangian in terms of the Goldstone boson fields composed in \tilde{U} reads [18]

$$\begin{aligned} \mathcal{L}_\phi &= -V_0 + V_1\langle\nabla_\mu U^\dagger\nabla^\mu U\rangle + (V_2 + \mathcal{B}V_3)\langle\chi(U + U^\dagger)\rangle - i\mathcal{A}V_2\langle U - U^\dagger\rangle \\ &+ \mathcal{A}V_3\langle U + U^\dagger\rangle + V_4\langle U\nabla_\mu U^\dagger\rangle\langle U^\dagger\nabla^\mu U\rangle. \end{aligned} \quad (2.8)$$

Here $\chi = 2B_0\text{diag}(m_u\cos\varphi_u, m_d\cos\varphi_d, m_s\cos\varphi_s)$. To leading order, \mathcal{A} and \mathcal{B} are given as

$$\mathcal{A} = \frac{V_0^{(2)}}{V_2^{(0)}}\bar{\theta}_0 + \mathcal{O}(\delta^4), \quad \mathcal{B} = \frac{V_3^{(1)}}{V_2^{(0)}}\bar{\theta}_0 + \mathcal{O}(\delta^6). \quad (2.9)$$

After vacuum alignment, the V_i coefficients are now functions of $\bar{\theta}_0 + \sqrt{6}\eta_0/F_0$. Further, the normalization of the kinetic terms in the Lagrangian (2.3) provides

$$V_1(0) = V_2(0) = \frac{F_\pi^2}{4}, \quad V_4(0) = \frac{1}{12}(F_0^2 - F_\pi^2). \quad (2.10)$$

In principle, the coupling of the η_0 singlet is different from F_π because the subgroup $U(3)_V$ does not present a nonet symmetry. However, in the large N_c -limit $F_0 = F_\pi$. Moreover, the quantity of $\bar{\theta}_0$ can be denoted in terms of physical quantities [21]

$$\bar{\theta}_0 = \left[1 + \frac{4V_0^{(2)}}{F_\pi^2} \frac{4M_K^2 - M_\pi^2}{M_\pi^2(2M_K^2 - M_\pi^2)} \right]^{-1} \theta_0. \quad (2.11)$$

Here, we note that $\bar{\theta}_0 = \mathcal{O}(\delta^2)$, and take $1/N_c = \mathcal{O}(\delta^2)$ as counting rules [19]. More detail and information on the formalism used in the work can be found in e.g. in refs. [18, 20].

We now turn to the baryon sector of the effective Lagrangian. In the $SU(3)$ flavor representation the spin-1/2 anti-symmetric triplet and symmetric sextet charmed baryon states are denoted as in the following matrices, respectively,

$$B_{\bar{3}} = \begin{pmatrix} 0 & \Lambda_c^+ & \Xi_c^+ \\ -\Lambda_c^+ & 0 & \Xi_c^0 \\ -\Xi_c^+ & -\Xi_c^0 & 0 \end{pmatrix}, \quad B_6 = \begin{pmatrix} \Sigma_c^{++} & \frac{\Sigma_c^+}{\sqrt{2}} & \frac{\Xi_c'^+}{\sqrt{2}} \\ \frac{\Sigma_c^+}{\sqrt{2}} & \Sigma_c^0 & \frac{\Xi_c'^0}{\sqrt{2}} \\ \frac{\Xi_c'^+}{\sqrt{2}} & \frac{\Xi_c'^0}{\sqrt{2}} & \Omega_c^0 \end{pmatrix}.$$

Similarly to the mesonic Lagrangian one can write down the most general effective Lagrangian for the charmed baryon multiplets. Here, we only present the terms pertinent to the calculation. In the quark mass and momentum expansion, the relevant free and interaction Lagrangians up to the second chiral order are given by [13, 15, 18, 22, 24],

$$\begin{aligned} \mathcal{L}_{\phi B, \text{free}}^{(1)} &= \frac{1}{2} \langle \bar{B}_{\bar{3}} (i\not{D} - m_{\bar{3}}) B_{\bar{3}} \rangle + \langle \bar{B}_6 (i\not{D} - m_6) B_6 \rangle, \\ \mathcal{L}_{\phi B, \text{int}}^{(1)} &= \frac{g_1}{2} \langle \bar{B}_6 \not{\psi} \gamma_5 B_6 \rangle + \frac{g_2}{2} \left[\langle \bar{B}_6 \not{\psi} \gamma_5 B_{\bar{3}} \rangle + h.c. \right] + \frac{g_6}{2} \langle \bar{B}_{\bar{3}} \not{\psi} \gamma_5 B_{\bar{3}} \rangle \\ &\quad + \frac{g_1}{2} \langle \bar{B}_6 \gamma^\mu \gamma_5 B_6 \rangle \langle u_\mu \rangle + \frac{g_2}{2} \left[\langle \bar{B}_6 \gamma^\mu \gamma_5 B_{\bar{3}} \rangle + h.c. \right] \langle u_\mu \rangle + \frac{g_6}{2} \langle \bar{B}_{\bar{3}} \gamma^\mu \gamma_5 B_{\bar{3}} \rangle \langle u_\mu \rangle, \\ \mathcal{L}_{\bar{3}\bar{3}}^{(2)} &= w_{16/17} \langle \bar{B}_{\bar{3}} \sigma^{\mu\nu} F_{\mu\nu}^+ B_{\bar{3}} \rangle + w_{18} \langle \bar{B}_{\bar{3}} \sigma^{\mu\nu} B_{\bar{3}} \rangle \langle F_{\mu\nu}^+ \rangle + b_{D/F} \langle \bar{B}_{\bar{3}} \tilde{\chi}_+ B_{\bar{3}} \rangle + b_0 \langle \bar{B}_{\bar{3}} B_{\bar{3}} \rangle \langle \tilde{\chi}_+ \rangle \\ &\quad + iw_{10/11} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_{\bar{3}} \tilde{\chi}_- B_{\bar{3}} \rangle + iw_{12} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_{\bar{3}} B_{\bar{3}} \rangle \langle \tilde{\chi}_- \rangle \\ &\quad + i \left(w'_{13/14} \bar{\theta}_0 + w_{13/14} \frac{\sqrt{6}}{F_0} \eta_0 \right) \langle \bar{B}_{\bar{3}} \sigma^{\mu\nu} \gamma_5 F_{\mu\nu}^+ B_{\bar{3}} \rangle \\ &\quad + i \left(w'_{15} \bar{\theta}_0 + w_{15} \frac{\sqrt{6}}{F_0} \eta_0 \right) \langle \bar{B}_{\bar{3}} \sigma^{\mu\nu} \gamma_5 B_{\bar{3}} \rangle \langle F_{\mu\nu}^+ \rangle, \\ \mathcal{L}_{66}^{(2)} &= w_{16/17} \langle \bar{B}_6 \sigma^{\mu\nu} F_{\mu\nu}^+ B_6 \rangle + w_{18} \langle \bar{B}_6 \sigma^{\mu\nu} B_6 \rangle \langle F_{\mu\nu}^+ \rangle + b_{D/F} \langle \bar{B}_6 \tilde{\chi}_+ B_6 \rangle + b_0 \langle \bar{B}_6 B_6 \rangle \langle \tilde{\chi}_+ \rangle \\ &\quad + iw_{10/11} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_6 \tilde{\chi}_- B_6 \rangle + iw_{12} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_6 B_6 \rangle \langle \tilde{\chi}_- \rangle \\ &\quad + i \left(w'_{13/14} \bar{\theta}_0 + w_{13/14} \frac{\sqrt{6}}{F_0} \eta_0 \right) \langle \bar{B}_6 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu}^+ B_6 \rangle \\ &\quad + i \left(w'_{15} \bar{\theta}_0 + w_{15} \frac{\sqrt{6}}{F_0} \eta_0 \right) \langle \bar{B}_6 \sigma^{\mu\nu} \gamma_5 B_6 \rangle \langle F_{\mu\nu}^+ \rangle, \\ \mathcal{L}_{\bar{6}\bar{3}}^{(2)} &= w_{16/17} \langle \bar{B}_6 \sigma^{\mu\nu} F_{\mu\nu}^+ B_{\bar{3}} \rangle + b_{D/F} \langle \bar{B}_6 \tilde{\chi}_+ B_{\bar{3}} \rangle + iw_{10/11} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_6 \tilde{\chi}_- B_{\bar{3}} \rangle \\ &\quad + iw_{13/14} \frac{\sqrt{6}}{F_0} \eta_0 \langle \bar{B}_6 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu}^+ B_{\bar{3}} \rangle + h.c., \end{aligned} \quad (2.12)$$

where the relevant building blocks are

$$\begin{aligned}
\tilde{\chi}_- &= \chi_- - i\mathcal{A}(U + U^\dagger) - i\mathcal{B}\chi_+, \\
\tilde{\chi}_+ &= \chi_+ - i\mathcal{A}(U - U^\dagger) - i\mathcal{B}\chi_-, \\
D_\mu B &= \partial_\mu B + \Gamma_\mu B + B\Gamma_\mu^T, \\
\Gamma_\mu &= \frac{1}{2}[u^\dagger(\partial_\mu - ir_\mu)u + u(\partial_\mu - il_\mu)u^\dagger], \\
u &= i[u^\dagger(\partial_\mu - ir_\mu)u - u(\partial_\mu - il_\mu)u^\dagger].
\end{aligned}
\tag{2.13}$$

The charge matrix for the singly-charmed baryons is $Q_h = \text{diag}(1, 0, 0)$, while for the light quarks the charge matrix is $Q_l = \text{diag}(2/3, -1/3, -1/3)$. We use $w_{10/11} + 3w_{12} = w'_{10}$ as in ref. [21].

As can be seen from the contributing Lagrangians, there are quite number of low-energy constants (LECs). The meson-baryon coupling constants g_i ($i = 1, \dots, 6$), the symmetry-breaking LECs b_D and b_F as well as the LECs $w_{16/17}, w_{18}$ related to the CP-conserving electromagnetic response can all be taken from earlier studies of different observables, as detailed in section 4.

This leaves us with the yet undetermined LECs $w'_{10}, w'_{13/14}, w'_{15}$ and $w_{13/14}, w_{15}$. As will be shown, we can fix $w_{13/14}, w_{15}$ from recent lattice results QCD for the neutron and proton electric dipole moments, d_n and d_p , respectively. The remaining of these LECs will be varied as $0_{-0.5}^{+0.5} \text{ GeV}^{-1}$, that is within a natural range. This naive dimensional analysis should be eventually overcome by a more sophisticated modeling of the LECs or invoking further lattice QCD results. Having fixed/estimated all the LECs will then allow to estimate the CP-violating contributions to the singly-charmed baryons induced by the θ -term.

3 CP-violating electromagnetic form factor

The electromagnetic form factors of a baryon are defined via the matrix element of the electromagnetic current,

$$\begin{aligned}
\langle B(p_f) | J_{\text{em}}^\mu | B(p_i) \rangle &= \bar{u}(p_f) \left[\gamma^\mu F_1(q^2) - \frac{iF_2(q^2)}{2m_B} \sigma^{\mu\nu} q_\nu \right. \\
&\quad \left. + i(\gamma^\mu q^2 \gamma_5 - 2m_B q^\mu \gamma_5) F_A(q^2) - \frac{F_3(q^2)}{2m_B} \sigma^{\mu\nu} q_\nu \gamma_5 \right] u(p_i),
\end{aligned}
\tag{3.1}$$

with $q^2 = (p_f - p_i)^2$ the invariant momentum transfer squared, m_B the baryon mass and J_{em}^μ the electromagnetic current. Here, $F_1(q^2)$ and $F_2(q^2)$ are the P- and CP-conserving Dirac and Pauli form factors, respectively. $F_A(q^2)$ denotes the P-violating anapole form factor, and $F_3(q^2)$, which will be considered throughout this work, the P- and CP-violating electric dipole form factor. The electric dipole moment of the baryon B is then given by

$$d_B = \frac{F_{3,B}(0)}{2m_B}.
\tag{3.2}$$

In what follows, we will use the effective Lagrangian to calculate the CP-violating form factor of the singly-charmed baryons at next-to-leading (NLO) order, which includes tree as well as loop diagrams as shown in figure 1, where we display the corresponding

Feynman diagrams. Tree-level diagrams at leading order are presented in (a) and (b). One-loop diagrams at order $\mathcal{O}(\delta^2)$ and $\mathcal{O}(\delta^3)$ in (c)-(d), and (e)-(h), respectively. The type of diagrams in (g)-(h) with pionic or kaonic loops of the antitriplet and the sextet charmed baryons are canceling each other, thus they are not displayed here.

We show different combinations of the charmed baryon states from anti-triplet and sextet multiplets considered throughout the calculation in figure 2.

The results obtained for the form factor $F_3(q^2)$ of the charmed baryons coming from the tree-level diagrams are collected in table 1 with

$$\alpha = \frac{576V_0^{(2)}V_3^{(1)}}{(F_0F_\pi M_{\eta_0})^2}. \quad (3.3)$$

As usual in the EOMS scheme, the loop contributions are rather lengthy expression. Let us discuss the case of the Λ_c^+ . The one-loop contribution can be written as, cf. figure 1,

$$\begin{aligned} F_{3,\Lambda_c^+}^{\text{loop}}(q^2) &= \sum_{i=1}^2 \frac{e\bar{\theta}_0 V_0^{(2)} \tilde{m}}{\pi^2 F_\pi^4} \frac{1}{(4\tilde{m}^2 - q^2)} \\ &\times \left[C_{cd}^i(m_i(\tilde{m} + m_i)) \left(2J_i^{cd}(\tilde{m}^2, m_i^2, M^2) - 2J_i^{cd}(q^2, M^2, M^2) \right) \right. \\ &\quad \left. + (2M^2 + 2\tilde{m}^2 - 2m_i^2 - q^2) J_i^{cd}(\tilde{m}^2, \tilde{m}^2, q^2, M^2, m_i^2, M^2) \right] \\ &+ \sum_{i=3}^4 \frac{e\bar{\theta}_0 V_0^{(2)}}{\pi^2 F_\pi^4} \frac{1}{(4\tilde{m}^2 - q^2)} \left[C_{ef}^i \left(-J_i^{ef}(M_i^2)(4\tilde{m}^2 - q^2) + J_i^{ef}(\tilde{m}^2)(4\tilde{m}^2 - q^2) \right) \right. \\ &\quad - (M_i^2(q^2 + 4\tilde{m}^2) - 4\tilde{m}^2 q^2) J_i^{ef}(\tilde{m}^2, \tilde{m}^2, M_i^2) + 8\tilde{m}^2(M_i^2 - 2\tilde{m}^2) J_i^{ef}(q^2, \tilde{m}^2, \tilde{m}^2) \\ &\quad \left. + 4\tilde{m}^2 M_i^2(2M_i^2 - 8\tilde{m}^2 + q^2) J_i^{ef}(\tilde{m}^2, \tilde{m}^2, q^2, \tilde{m}^2, M^2, \tilde{m}^2) \right] \\ &+ \sum_{i=5}^7 \frac{e\bar{\theta}_0 V_0^{(2)}}{\pi^2 F_\pi^4} \frac{1}{(4\tilde{m}^2 - q^2)} \left[C_{ef}^i \left(-J_i^{ef}(M_i^2)(4\tilde{m}^2 - q^2) + J_i^{ef}(m_i^2)(4\tilde{m}^2 - q^2) \right) \right. \\ &\quad - (M_i^2(4\tilde{m}m_i + q^2) + (m_i + \tilde{m})(4\tilde{m}^2 m_i - m_i q^2 - \tilde{m}(4m_i^2 + q^2))) J_i^{ef}(\tilde{m}^2, m_i^2, M_i^2) \\ &\quad - 4\tilde{m}(\tilde{m} + m_i)(\tilde{m}^2 + m_i^2 - M_i^2) J_i^{ef}(q^2, m_i^2, m_i^2) + 2\tilde{m}(\tilde{m} + m_i) \\ &\quad \times (2M_i^4 + (\tilde{m}^2 - m_i^2)(2\tilde{m}^2 - 2m_i^2 - q^2) \\ &\quad \left. + M_i^2(q^2 - 4\tilde{m}^2 - 4m_i^2)) J_i^{ef}(\tilde{m}^2, \tilde{m}^2, q^2, m_i^2, M_i^2, m_i^2) \right] \\ &+ \sum_{i=8}^{10} \frac{e\bar{\theta}_0 V_0^{(2)}}{\pi^2 F_\pi^4} \frac{1}{(4\tilde{m}^2 - q^2)} \left[C_{ef}^i \left(-J_i^{ef}(M_i^2)(4\tilde{m}^2 - q^2) + J_i^{ef}(m_i^2)(4\tilde{m}^2 - q^2) \right) \right. \\ &\quad + (\tilde{m}^2 q^2 - 4\tilde{m}^3 m_i + q^2(m_i^2 - M_i^2) + 2\tilde{m}m_i(q^2 + 2m_i^2 - 2M_i^2)) J_i^{ef}(\tilde{m}^2, m_i^2, M_i^2) \\ &\quad - 4\tilde{m}(\tilde{m} + m_i)(\tilde{m}^2 + m_i^2 - M_i^2) J_i^{ef}(q^2, m_i^2, m_i^2) + 2\tilde{m}(\tilde{m} + m_i) \\ &\quad \times (2M_i^4 + 2\tilde{m}^4 + M_i^2(q^2 - 4m_i^2) + m_i^2(2m_i^2 + q^2) \\ &\quad \left. - \tilde{m}^2(4M_i^2 + 4m_i^2 + q^2)) J_i^{ef}(\tilde{m}^2, \tilde{m}^2, q^2, m_i^2, M_i^2, m_i^2) \right] \\ &+ \frac{16e\bar{\theta}_0 V_0^{(2)}}{\pi^2 F_\pi^2 F_0^2} \left[C_{gh}^{11} \left(J_{11}^{gh}(M^2) - J_{11}^{gh}(\tilde{m}^2) - (M^2 - 4\tilde{m}^2) J_{11}^{gh}(\tilde{m}^2, M^2) \right) \right], \quad (3.4) \end{aligned}$$

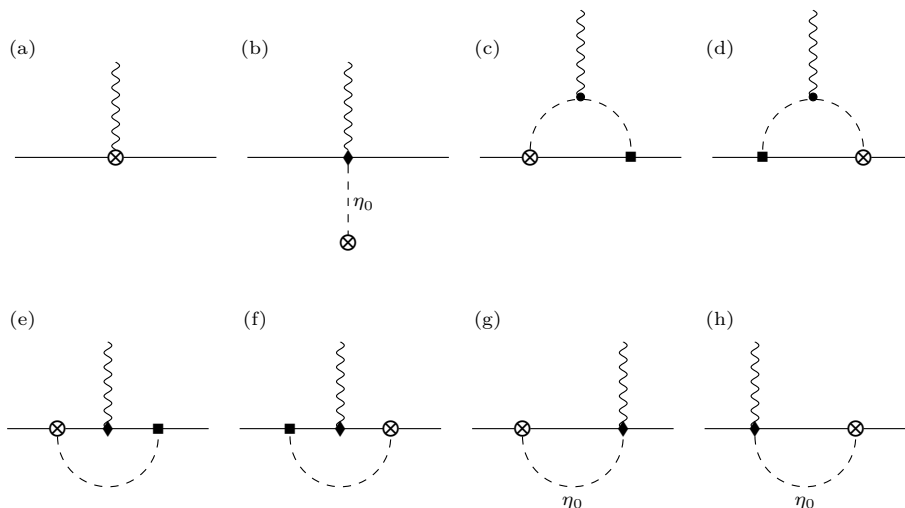


Figure 1. CP-violating contributions of the spin-1/2 charmed baryons. Solid lines correspond to contribution from either spin-1/2 anti-triplet or sextet multiplets of charmed baryons. Filled circles are second-order mesonic vertices, squares and diamonds represent vertices generated by the first and second order meson-baryon Lagrangian, respectively. CP-violating vertices are denoted by \otimes .

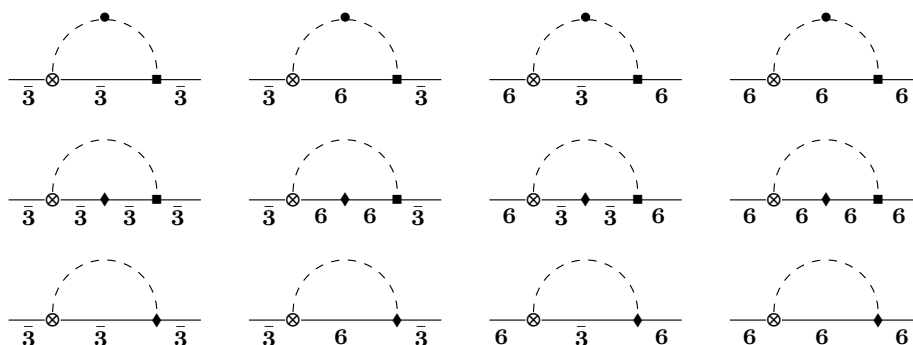


Figure 2. Different combinations of the spin-1/2 anti-triplet and sextet charmed baryons contributing to $F_3(q^2)$.

with m_i , \tilde{m}_i and M_i denoting the masses of the corresponding internal and external baryons and meson running in the loop, for notational simplicity. In the case at hand, $\tilde{m} = m_{\Lambda_c^+}$. The $J(m_i, M_i, q^2)$ functions can be reduced to the scalar loop functions given in appendix A, and the labels cd , ef and gh refer to the types of diagrams shown in figure 1. The corresponding coefficients C_{cd} , C_{ef} and C_{gh} for the Λ_c^+ together with the intermediate meson-baryon states are shown in table 2, the corresponding tables for the other particles can be found in appendix B. A MATHEMATICA notebook with these loop functions can be obtained from the first author of this paper.

States	Contributions	
$B_{\bar{3}}$	Λ_c^+	$e\bar{\theta}_0 m_{\Lambda_c} [2\alpha(w_{13/14} + 2w_{15}) + 8(w'_{13/14} + 2w'_{15})]$
	Ξ_c^+	$e\bar{\theta}_0 m_{\Xi_c} [2\alpha(w_{13/14} + 2w_{15}) + 8(w'_{13/14} + 2w'_{15})]$
	Ξ_c^0	$e\bar{\theta}_0 m_{\Xi_c} 4(\alpha w_{15} + 4w'_{15})$
B_6	Σ_c^{++}	$e\bar{\theta}_0 m_{\Sigma_c} [2\alpha(w_{13/14} + w_{15}) + 8(w'_{13/14} + w'_{15})]$
	Σ_c^+	$e\bar{\theta}_0 m_{\Sigma_c} [\alpha(w_{13/14} + 2w_{15}) + 4(w'_{13/14} + 2w'_{15})]$
	Σ_c^0	$e\bar{\theta}_0 m_{\Sigma_c} 2(\alpha w_{15} + 4w'_{15})$
	$\Xi_c'^+$	$e\bar{\theta}_0 m_{\Xi_c'} [\alpha(w_{13/14} + 2w_{15}) + 4(w'_{13/14} + 2w'_{15})]$
	$\Xi_c'^0$	$e\bar{\theta}_0 m_{\Xi_c'} 2(\alpha w_{15} + 4w'_{15})$
	Ω_c^0	$e\bar{\theta}_0 m_{\Omega_c} 2(\alpha w_{15} + 4w'_{15})$

Table 1. Tree-level contribution to the $F_3(q^2)$ of the charmed baryons.

Diagram type	number	meson-baryon state	Coefficient	
(c), (d)	1	Ξ_c^0, K^\pm	$2g_6 b_{D/F}$	
	2	$\Xi_c'^0, K^\pm$	$g_2 b_{D/F}$	
(e), (f)	3	Λ_c^+, η_8	$\frac{8}{3}g_6 b_{D/F}(w_{16/17} + 2w_{18})$	
	4	Λ_c^+, η_0	$\frac{32}{3}\beta g_6(w_{16/17} + 2w_{18})$	
	5	Ξ_c^+, K^0	$4g_6 b_{D/F}(w_{16/17} + 2w_{18})$	
	6	$\Xi_c'^0, K^\pm$	$2g_2 b_{D/F} w_{18}$	
	7	$\Xi_c'^+, K^0$	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$	
	8	Σ_c^0, π^\pm	$4g_2 b_{D/F} w_{18}$	
	9	Σ_c^+, π^0	$2g_2 b_{D/F}(w_{16/17} + 2w_{18})$	
	10	Σ_c^{++}, π^\pm	$4g_2 b_{D/F}(w_{16/17} + w_{18})$	
	(g), (h)	11	Λ_c^+, η_0	$\beta(w_{13/14} + 2w_{15})$

Table 2. Loop contribution to the $F_3(q^2)$ of the Λ_c^+ baryon with $\beta = (b_{D/F} + b_0 + 3w'_{10})$.

4 Results

First, we must fix parameters. The pion decay constant is taken as $F_\pi = 92.2 \text{ MeV}$. In what follows, due to the lack of data from the charmed meson sector, we make recourse to the ground state baryon octet as much as possible to fix as many LECs as possible. While this is an approximation, we expect that we are estimating at least the right order of magnitude of the EDMs of the charmed baryons. Consequently, two symmetry-breaking LECs in the baryon sector can be obtained from baryon mass splittings. We use $b_D = -0.606 \text{ GeV}^{-1}$ and $b_F = -0.209 \text{ GeV}^{-1}$ [23, 24]. The tree-level contributions can be expressed in terms of two independent linear combinations of unknown LECs as $\alpha(w_{13/14} + 4w'_{13/14})$ and $\alpha w_{15} + 4w'_{15}$, cf. table 1. The loop contributions are also dependent on unknown LECs, viz., w'_{10} , $w_{13/14}$ and w_{15} . The conventional magnetic moment couplings, w_{18} is taken equal to $w_{16/17} = 0.40$, determined from fits to calculations to baryon magnetic moments in [25, 26].

Further, $V_0^{(2)} = -5 \times 10^{-4} \text{ GeV}^4$ and $V_3^{(1)} = 3.5 \times 10^{-4} \text{ GeV}^2$ are the values obtained from an analysis of $\eta - \eta'$ mixing in U(3) chiral perturbation theory [27]. The various baryon-meson couplings are taken from refs. [13, 14], $g_1 = 0.98$, $g_2 = -0.60$, $g_3 = 0.85$, and $g_4 = 1.04$. Because of the forbidden $B_3 B_3 \phi$ -vertex, we have $g_6 = 0$. We use the physical masses of the pertinent mesons and baryons running in the corresponding loops, cf. tables 4–11.

As the unknown LECs cannot be parameterized such a common constant as in [24], since the combinations coming from different particles are different, they have to be considered individually. Using the lattice data from [28] at physical pion mass, we use the neutron dipole moment to fix βw_{15} from the Ξ_c^0 by comparing the loop contributions. With that, we can use the proton electric dipole moment to determine $\beta w_{13/14}$ from the Λ_c^+ . We get

$$\beta w_{13/14} = -0.00435 \text{ GeV}^{-1}, \quad \beta w_{15} = 0.00175 \text{ GeV}^{-1}. \quad (4.1)$$

With these obtained values, we take the variation of w'_{10} , $w'_{13/14}$ and w'_{15} , and calculate the CP-violating form factor $F_3(q^2)$ for the singly-charmed baryons in the range $q^2 \simeq 0.05 \dots 0.3 \text{ GeV}^2$ as given in tables 12–14. We are well aware that there are other determinations of d_p and d_n in the literature, see e.g. refs. [29, 30], and that there is an on-going debate on the axial rotation in the finite volume (mixing between the form factors F_2 and F_3 , see e.g. ref. [31]). However, since our study is largely exploratory, we do not explore the whole possible parameter space.

The electric dipole moments for the various baryons are collected in table 3. As there is a sizeable uncertainty induced by the unknown LECs, we refrain from performing a systematic error analysis accounting e.g. for the effects of higher orders in the chiral expansion. Hopefully, lattice QCD will be able to supply pertinent information on the LECs so that more accurate predictions can be made.

5 Conclusion

In this paper, we have performed a one-loop calculation of the CP-violating form factor $F_3(q^2)$ and the corresponding electric dipole moments of the spin-1/2 singly-charmed

	Λ_c^+	Ξ_c^+	Ξ_c^0	Σ_c^{++}	Σ_c^+	Σ_c^0	$\Xi_c^{\prime+}$	$\Xi_c^{\prime0}$	Ω_c^0
Set 1	0.0476	0.0470	0.0294	0.0047	0.0053	0.0058	0.0007	0.0085	0.0067
Set 2	0.0011	0.0005	-0.0015	-0.0090	-0.0049	-0.0010	-0.0097	0.0015	-0.0003
Set 3	-0.0454	-0.0460	-0.0324	-0.0228	-0.0153	-0.0078	-0.0202	-0.0053	-0.0074

Table 3. Electric dipole moments for the singly-charmed baryons in units of $e\theta_0$ fm. Set 1,2,3 refers to $w'_{10} = w'_{13/14} = w'_{15} = -0.5, 0, +0.5$, in order.

baryons, where the mechanism of the CP violation is the QCD θ -term. Not all the appearing low-energy constants could be fixed from experimental or lattice QCD data, so the resulting predictions show a spread, cf. table 3 and the tables in appendix C. We hope that with more lattice QCD studies on strong CP violations, these LECs can be determined and more accurate predictions can be made, not to mention possible experimental determinations.

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A Scalar loop integrals

The scalar loop integrals of one-, two-, and three-point functions which are used for the calculation of the diagrams are given by

$$\begin{aligned}
 J_0(m^2) &= \frac{(2\pi\mu)^{4-d}}{i\pi^2} \int \frac{d^d k}{k^2 - m^2 + i0^+}, \\
 J_0(p^2, m_1^2, m_2^2) &= \frac{(2\pi\mu)^{4-d}}{i\pi^2} \int \frac{d^d k}{[k^2 - m_1^2 + i0^+][(k+p)^2 - m_2^2 + i0^+]}, \\
 J_0(p_i^2, (p_f - p_i)^2, p_f^2, m_1^2, m_2^2, m_3^2) &= \frac{(2\pi\mu)^{4-d}}{i\pi^2} \int \frac{d^d k}{[k^2 - m_1^2 + i0^+][(k-p_i)^2 - m_2^2 + i0^+][(k-p_f)^2 - m_3^2 + i0^+]}.
 \end{aligned}$$

B Loop contributions

All one-loop contributions to the various baryons take the form as given in eq. (3.4). In this appendix, we collect the corresponding intermediate meson-baryon states and the values of the coefficients C^{cd} , C^{ef} and C^{gh} for the baryons not given in the main text.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	Ξ_c^0, π^\pm	$g_6 b_{D/F}$
	2	Ω_c^0, K^\pm	$g_2 b_{D/F}$
	3	Σ_c^{++}, K^\pm	$g_2 b_{D/F}$
	4	$\Xi_c^{\prime 0}, \pi^\pm$	$g_2 b_{D/F}$
(e), (f)	5	Ξ_c^+, η_8	$g_6 b_{D/F}(w_{16/17} + 2w_{18})$
	6	Ξ_c^+, η_0	$\beta g_6(w_{16/17} + 2w_{18})$
	7	Ξ_c^+, π^0	$g_6 b_{D/F}(w_{16/17} + 2w_{18})$
	8	$\Xi_c^{\prime 0}, \pi^\pm$	$g_2 b_{D/F} w_{18}$
	9	$\Xi_c^{\prime +}, \eta_8$	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	10	Σ_c^+, K^0	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	11	$\Xi_c^{\prime +}, \pi^0$	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	12	Σ_c^{++}, K^\pm	$g_2 b_{D/F}(w_{16/17} + w_{18})$
	13	Ω_c^0, K^\pm	$g_2 b_{D/F} w_{18}$
(g), (h)	14	Ξ_c^+, η_0	$\beta(w_{13/14} + 2w_{15})$

Table 4. Loop contribution to the $F_3(q^2)$ of the Ξ_c^+ baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	Λ_c^+, K^\pm	$g_6 b_{D/F}$
	2	Ω_c^0, K^\pm	$g_2 b_{D/F}$
	3	Ξ_c^+, π^\pm	$g_6 b_{D/F}$
	4	Σ_c^+, K^\pm	$g_2 b_{D/F}$
	5	$\Xi_c^{\prime +}, \pi^\pm$	$g_2 b_{D/F}$
(e), (f)	6	Ξ_c^0, η_8	$g_6 b_{D/F} w_{18}$
	7	Ξ_c^0, η_0	$\beta g_6 w_{18}$
	8	Ξ_c^0, π^0	$g_6 b_{D/F} w_{18}$
	9	$\Xi_c^{\prime +}, \pi^\pm$	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	10	Σ_c^0, K^0	$g_2 b_{D/F} w_{18}$
	11	$\Xi_c^{\prime 0}, \eta_8$	$g_2 b_{D/F} w_{18}$
	12	$\Xi_c^{\prime 0}, \pi^0$	$g_2 b_{D/F} w_{18}$
	13	Σ_c^+, K^\pm	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	14	Ω_c^0, K^0	$g_2 b_{D/F} w_{18}$
(g), (h)	15	Ξ_c^0, η_0	βw_{15}

Table 5. Loop contribution to the $F_3(q^2)$ of the Ξ_c^0 baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	$\Xi_c^{\prime+}, K^\pm$	$g_1 b_{D/F}$
	2	Σ_c^+, π^\pm	$g_1 b_{D/F}$
	3	Ξ_c^+, K^\pm	$g_2 b_{D/F}$
	4	Λ_c^+, π^\pm	$g_2 b_{D/F}$
(e), (f)	5	Σ_c^{++}, η_8	$g_1 b_{D/F}(w_{16/17} + w_{18})$
	6	Σ_c^{++}, η_0	$\beta g_1(w_{16/17} + w_{18})$
	7	Σ_c^{++}, π^0	$g_1 b_{D/F}(w_{16/17} + w_{18})$
	8	Ξ_c^+, K^\pm	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	9	Λ_c^0, π^\pm	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
(g), (h)	10	Σ_c^{++}, η_0	$\beta(w_{13/14} + w_{15})$

Table 6. Loop contribution to the $F_3(q^2)$ of the Σ_c^{++} baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	$\Xi_c^{\prime0}, K^\pm$	$g_1 b_{D/F}$
	2	Ξ_c^0, K^\pm	$g_2 b_{D/F}$
(e), (f)	3	Σ_c^+, η_8	$g_1 b_{D/F}(w_{16/17} + 2w_{18})$
	4	Σ_c^+, η_0	$\beta g_1(w_{16/17} + 2w_{18})$
	5	Ξ_c^+, K^0	$g_2 b_{D/F}(w_{16/17} + w_{18})$
	6	Ξ_c^0, K^\pm	$g_2 b_{D/F} w_{18}$
	7	Λ_c^0, π^0	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
(g), (h)	8	Σ_c^+, η_0	$\beta(w_{13/14} + 2w_{15})$

Table 7. Loop contribution to the $F_3(q^2)$ of the Σ_c^+ baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	Σ_c^+, π^\pm	$g_1 b_{D/F}$
	2	Λ_c^0, π^\pm	$g_2 b_{D/F}$
(e), (f)	3	Σ_c^0, η_8	$g_1 b_{D/F} w_{18}$
	4	Σ_c^0, η_0	$\beta g_1 w_{18}$
	5	Σ_c^0, π^0	$g_1 b_{D/F} w_{18}$
	6	Ξ_c^0, K^0	$g_2 b_{D/F} w_{18}$
	7	Λ_c^0, π^\pm	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
(g), (h)	8	Σ_c^0, η_0	βw_{15}

Table 8. Loop contribution to the $F_3(q^2)$ of the Σ_c^0 baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	Ω_c^0, K^\pm	$g_1 b_{D/F}$
	2	Σ_c^{++}, K^\pm	$g_1 b_{D/F}$
	3	$\Xi_c^{\prime 0}, \pi^\pm$	$g_1 b_{D/F}$
	4	Ξ_c^0, π^\pm	$g_2 b_{D/F}$
(e), (f)	5	$\Xi_c^{\prime +}, \eta_8$	$g_1 b_{D/F}(w_{16/17} + 2w_{18})$
	6	$\Xi_c^{\prime +}, \eta_0$	$\beta g_1(w_{16/17} + 2w_{18})$
	7	$\Xi_c^{\prime +}, \pi^0$	$g_1 b_{D/F}(w_{16/17} + 2w_{18})$
	8	Σ_c^+, K^0	$g_1 b_{D/F}(w_{16/17} + 2w_{18})$
	9	Ξ_c^+, η_8	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	10	Λ_c^+, K^0	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	11	Ξ_c^+, π^0	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	12	Ξ_c^0, π^\pm	$g_2 b_{D/F} w_{18}$
(g), (h)	13	$\Xi_c^{\prime +}, \eta_0$	$\beta(w_{13/14} + 2w_{15})$

Table 9. Loop contribution to the $F_3(q^2)$ of the $\Xi_c^{\prime +}$ baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	Σ_c^+, K^\pm	$g_1 b_{D/F}$
	2	$\Xi_c^{\prime +}, \pi^\pm$	$g_1 b_{D/F}$
	3	Λ_c^+, K^\pm	$g_2 b_{D/F}$
	4	Ξ_c^+, π^\pm	$g_2 b_{D/F}$
(e), (f)	5	$\Xi_c^{\prime 0}, \eta_8$	$g_1 b_{D/F} w_{18}$
	6	$\Xi_c^{\prime 0}, \eta_0$	$\beta g_1 w_{18}$
	7	$\Xi_c^{\prime 0}, \pi^0$	$g_1 b_{D/F} w_{18}$
	8	Σ_c^0, K^0	$g_1 b_{D/F} w_{18}$
	9	Ω_c^0, K^0	$g_1 b_{D/F} w_{18}$
	10	Λ_c^0, K^\pm	$g_2 b_{D/F}(w_{16/17} + 2w_{18})$
	11	Ξ_c^0, η_8	$g_2 b_{D/F} w_{18}$
	12	Ξ_c^0, π^0	$g_2 b_{D/F} w_{18}$
(g), (h)	13	$\Xi_c^{\prime 0}, \eta_0$	βw_{15}

Table 10. Loop contribution to the $F_3(q^2)$ of the $\Xi_c^{\prime 0}$ baryon.

Diagram type	Number	Meson-baryon state	Coefficient
(c), (d)	1	$\Xi_c^{\prime+}, K^\pm$	$g_1 b_{D/F}$
	2	Ξ_c^+, K^\pm	$g_2 b_{D/F}$
(e), (f)	3	Ω_c^0, η_8	$g_1 b_{D/F} w_{18}$
	4	Ω_c^0, η_0	$\beta g_1 w_{18}$
	5	Ξ_c^+, K^\pm	$g_2 b_{D/F} (w_{16/17} + 2w_{18})$
	6	Ξ_c^0, K^0	$g_2 b_{D/F} w_{18}$
(g), (h)	7	Ω_c^0, η_0	βw_{15}

Table 11. Loop contribution to the $F_3(q^2)$ of the Ω_c^0 baryon.

C Results for the CP-violating form factor

This appendix contains results for the loop contributions to the form factor $F_3(q^2)$ for the various baryons, for photon virtualities below $q^2 \simeq 0.3 \text{ GeV}^2$.

$q^2(\text{GeV}^2)$	Λ_c^+	Ξ_c^+	Ξ_c^0	Σ_c^{++}	Σ_c^+	Σ_c^0	$\Xi_c^{\prime+}$	$\Xi_c^{\prime0}$	Ω_c^0
0.0484	1.1028	1.1772	0.7362	-0.1150	0.1339	0.3832	0.0361	0.2102	0.1855
0.1024	1.1015	1.1764	0.7339	-0.0434	0.1359	0.3164	0.0452	0.2047	0.1861
0.1444	1.1004	1.1756	0.7323	-0.0175	0.1374	0.2943	0.0500	0.2027	0.1865
0.1936	1.0992	1.1747	0.7305	0.0021	0.1392	0.2789	0.0546	0.2014	0.1871
0.2500	1.0978	1.1735	0.7285	0.0181	0.1412	0.2679	0.0590	0.2007	0.1877
0.3136	1.0963	1.1722	0.7264	0.0319	0.1435	0.2598	0.0633	0.2006	0.1885

Table 12. Loop contribution to the $F_3(q^2)$ of the $B_{\bar{3}}$ and B_6 states for $w'_{10}, w'_{13/14}, w'_{15} = -0.5$.

$q^2(\text{GeV}^2)$	Λ_c^+	Ξ_c^+	Ξ_c^0	Σ_c^{++}	Σ_c^+	Σ_c^0	$\Xi_c^{\prime+}$	$\Xi_c^{\prime0}$	Ω_c^0
0.0484	0.0245	0.0121	-0.0414	-0.4594	-0.1246	0.2102	-0.2403	0.0253	-0.0108
0.1024	0.0232	0.0113	-0.0437	-0.3912	-0.1252	0.1417	-0.2339	0.0181	-0.0121
0.1444	0.0221	0.0105	-0.0453	-0.3680	-0.1257	0.1183	-0.2311	0.0147	-0.0130
0.1936	0.0209	0.0096	-0.0471	-0.3513	-0.1262	0.1015	-0.2289	0.0118	-0.0140
0.2500	0.0195	0.0085	-0.0491	-0.3388	-0.1268	0.0887	-0.2272	0.0094	-0.0152
0.3136	0.0180	0.0071	-0.0512	-0.3290	-0.1275	0.0786	-0.2259	0.0073	-0.0165

Table 13. Loop contribution to the $F_3(q^2)$ of the $B_{\bar{3}}$ and B_6 states for $w'_{10}, w'_{13/14}, w'_{15} = 0$.

$q^2(\text{GeV}^2)$	Λ_c^+	Ξ_c^+	Ξ_c^0	Σ_c^{++}	Σ_c^+	Σ_c^0	$\Xi_c^{\prime+}$	$\Xi_c^{\prime0}$	Ω_c^0
0.0484	-1.0545	-1.1538	-0.8155	-0.8065	-0.3837	0.0391	-0.5173	-0.1575	-0.2053
0.1024	-1.0558	-1.1546	-0.8177	-0.7416	-0.3869	-0.0310	-0.5135	-0.1665	-0.2083
0.1444	-1.0569	-1.1553	-0.8194	-0.7211	-0.3893	-0.0557	-0.5127	-0.1712	-0.2106
0.1936	-1.0581	-1.1563	-0.8212	-0.7075	-0.3921	-0.0741	-0.5129	-0.1757	-0.2133
0.2500	-1.0595	-1.1574	-0.8231	-0.6986	-0.3954	-0.0887	-0.5139	-0.1799	-0.2163
0.3136	-1.0610	-1.1588	-0.8253	-0.6927	-0.3991	-0.1008	-0.5156	-0.1841	-0.2196

Table 14. Loop contribution to the $F_3(q^2)$ of the $B_{\bar{3}}$ and B_6 states for $w'_{10}, w'_{13/14}, w'_{15} = 0.5$.

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